



**FIJI NATIONAL UNIVERSITY**

**College of Engineering, Science & Technology (CEST)**

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**SCHOOL OF MECHANICAL ENGINEERING**

**TRADE DIPLOMA IN MECHANICAL ENGINEERING**

**REE 592 HYDRO ENERGY SYSTEMS FINAL EXAMINATION Trimester 2 /2017**

**DURATION : 3 HOURS**

**Instructions to Students:**

01. You are allowed **10** minutes **EXTRA** reading time to *familiarize, evaluate* and *study* the requirements being asked in all the problems before starting to write your solutions.
02. Begin each question on a *fresh page*, avoid too many erasures and use both sides of the answer sheet.
03. Write your *candidate number* at the top of each attached answer sheet.
04. Write clearly the number(s) of the question(s) attempted on the top of each sheet.
05. Insert all written foolscap, graph paper, drawing paper, etc. in their correct sequence and secure with string.
06. *Candidates are warned not to open any lecture notes. Any attempt to do so and was caught shall be outright disqualified to sit in the Final Examination and the student shall be subject to academic disciplinary action.*
07. The paper consists of 2 parts A, four questions in B. Students must do all of A and B.. Check your paper thoroughly so that all parts are included.
08. Use black or blue ball pen in answering, pencils are not allowed, except for drawing figures.
09. Number of pages:6

**ATTEMPT ALL THE QUESTIONS IN Part A, Part B .**

Part A Short Answers All questions earn equal marks.

40 marks

Questions

1. What is involved in Hydro Power Energy Systems and the energy conversions in each case. 2 marks
  
2. Many studies have to be undertaken to establish a sustainable Hydro scheme, name the studies  
2 marks
  
3. Choose and explain 4 important components of a feasibility study 2 marks
  
4. Name the components of a typical small Hydro-electric power plant. Describe the interrelationships of these components of the same system. 2 marks
  
5. What are the pre-construction activities of such a project to site the mini hydro in locality A  
2 marks
  
6. What are the two most important components that a locality should have for sustainable hydro activity. 2 marks
  
7. Describe the types of turbines available and the process of choosing the right type for a particular site.  
2 marks
  
8. The catchment area of the hydro is the area above the weir supporting the continuous flow of water to the streams and the dam. List a few risks and the required maintenance aspects of the catchment area. 2 marks
  
9. Describe 3 Flow measurement methods and the equipment used. 2 marks

10. Describe what a weir is and its location and function. Discuss how the weir affects the SMH. Describe some maintenance steps for the weir. 2 marks

11. How is a hydro power turbine able to pump water back up to storage again. What is the purpose of such an arrangement? 2marks

12. Describe the process of feasibility study for a hydropower station. Describe the essence of each step. 2 marks

13. What types of bearings are used in mounting and running a Pelton wheel. Which bearings are able to withstand axial or thrust forces? Discuss how bearings are maintained for long life. 2 marks

14. The detailed design of a project is made after outline study for further consideration of the project. Describe the process and its components. 2 marks

15. What is Plant factor, the load factor and their importance 2 marks

16. Belts are tightened after proper alignment, discuss the correct tension of the belt after tightening. 2 marks

17. Financial evaluation, time value for money, annuity equation, net present value. Describe each of the terms and by examples provide values for a project. Example 9.5.1/8.4.2 2marks

18. Compare Internal Rate of Return( IRR) and Net Present Value (NPV) 2 marks

19. Describe Annuity , Bank loans and project considerations to be made for a new project. 2 marks

20. Turbine drives involve the following: shafts, Bearings, couplings pulleys, Flat and Vee belts. What are the issues to consider when making a choice of which type of coupling to use. 2 marks

Part B Answer all four (4) Questions each of equal marks

60 marks

Question 1. Calculation of area daily rainfall

- Name the methods of calculating rainfall in an area under survey?
- What is the effect of Run off on rainfall calculations?
- The following is provided for a site under survey. Site is divided into areas W,Y and Z. Find the average daily rainfall.

1 and 2 Area and Rainfall Total number of squares in A = squares (total) = 135

	Gauge W	Gauge Y	Gauge Z
Squares	58	8	69
Rainfall mm/yr	2000	2700	3000

Total catchment area =  $4.88 \times 10^6 \text{ m}^3$

Evaporation is given as  $1.42 \text{ m/yr}$

- There are many ways of taking head measurements for purpose of height  $h$ , calculations. Name three (3) types and describe the process.
- Describe three (3) types of head measuring equipment and how it is used. 15 marks

Question 2.

- Impulse turbines like the Pelton wheels are used a lot in MH applications. Name and describe the functions of each component of the turbine.
- Examine the forces acting on the bucket of the turbine and deduce the resultant force of the water jet.
- The runner and bucket and nozzle jet diameter are all related, provide dimension for the remaining components from a jet diameter of  $12 \text{ mm}$ ?
- Shaft diameter calculations

Belt tension  $T = 16.64 \text{ kN}$  Speed rpm =  $450 \text{ rpm}$

Rotational speed is  $= 2\pi \times \text{frequency} = 47.12 \text{ rad/sec}$

Turbine shaft power is  $= 71 \text{ kW}$  Turbine runner pcd  $= 0.2 \text{ m}$

From a sketch, deduce the Moments and forces acting and using ASME code with yield stress and ultimate strength, find the diameter of the shaft. 15 marks

Question 3

15 Marks

- a) Water jet velocity of  $30 \text{ m/s}$  and static head of  $150 \text{ m}$  provides power to a Pelton wheel turbine of  $600 \text{ mm}$  diameter. What is the power generated? What is the force acting on the wheel and the velocity of the bucket?
- b) Describe Reaction turbines.
- c) Describe the following terms used in hydro power
- |               |                            |              |
|---------------|----------------------------|--------------|
| ↓ Cavitation  | Closed loop pumped storage |              |
| ↓ Diversion   | Draft tube                 |              |
| ↓ Fish ladder | Impoundment                |              |
|               | Non powered dams           |              |
| ↓ Runner      | Tail race                  | Wicket gates |
- d) Describe and show the difference of laminar or streamline and turbulent flow?
- e) Explain the effects of friction on fluid flow and provide calculation as proof.

Question 4

15 Marks

- a) Describe the meaning of Present Value  $PV = \text{future value}/(1 + m)^n$
- b) What is the internal rate of return, IRR.  $NPV = 0$
- c) Using Tables provided determine whether The following scheme is viable.

Prefeasibility study of a scheme makes quick estimates for a hydro scheme as follows

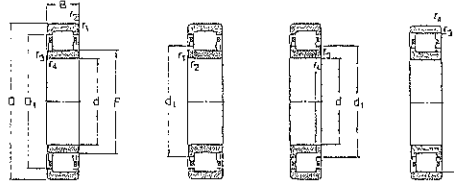
Revenue is  $\$20000$  each year for 15 years. Expenditure is start-up cost at  $\$120,000$  and yearly expenditure of  $\$8000$ . Calculate the NPV for the scheme @  $12\%$  discount factor and comment.

d) A  $12 \text{ kW}$  MHP for grain milling is proposed with a start-up cost of  $\$20,000$  and a discount rate of  $20\%$ .

Annual earnings of  $\$7000$  and maintenance costs of  $\$1400/\text{yr}$

END

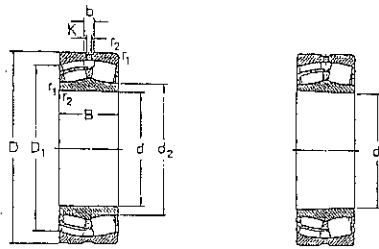
Cylindrical roller bearings  
single row  
d 75-80 mm



Principal dimensions	Basic load ratings		Fatigue load limit $P_0$	Speed ratings Lubrication grease or oil	Mass kg	Designation			
	dynamic $C_d$	static $C_0$							
d	D	B							
mm			N	N	r/min				
75	115	20	58 000	71 000	8 500	5 600	4 700	0,74	NU 1015
	130	25	130 000	156 000	20 400	4 200	5 200	1,25	NU 215 EC
	130	35	130 000	156 000	20 400	4 200	5 200	1,30	NJ 215 EC
	130	25	130 000	156 000	20 400	4 200	5 200	1,30	NUP 215 EC
	130	35	130 000	156 000	20 400	4 200	5 200	1,25	N 215 EC
	130	31	161 000	208 000	27 000	4 500	5 300	1,60	NU 2215 EC
	130	31	161 000	208 000	27 000	4 500	5 300	1,60	NJ 2215 EC
	130	31	161 000	208 000	27 000	4 500	5 300	1,65	NUP 2215 EC
	160	37	242 000	265 000	33 500	3 400	4 000	1,30	NU 315 EC
	160	37	242 000	265 000	33 500	3 400	4 000	1,30	NJ 315 EC
	160	37	242 000	265 000	33 500	3 400	4 000	1,45	NUP 315 EC
	160	37	242 000	265 000	33 500	3 400	4 000	1,30	N 315 EC
	180	35	330 000	400 000	50 000	3 400	4 000	4,30	NU 2315 EC
	180	35	330 000	400 000	50 000	3 400	4 000	5,00	NJ 2315 EC
	180	35	330 000	400 000	50 000	3 400	4 000	5,10	NUP 2315 EC
	180	45	254 000	280 000	34 000	3 400	4 000	6,25	NU 415
	180	45	254 000	280 000	34 000	3 400	4 000	6,40	NJ 415
80	125	22	88 000	81 500	10 400	5 300	6 200	0,98	NU 1016
	140	26	138 000	169 000	21 200	4 000	4 600	1,80	NU 216 EC
	140	26	138 000	169 000	21 200	4 000	4 600	1,55	NJ 216 EC
	140	26	138 000	169 000	21 200	4 000	4 600	1,60	NUP 216 EC
	140	26	138 000	169 000	21 200	4 000	4 600	1,50	N 216 EC
	140	33	187 000	245 000	31 000	4 000	4 800	2,00	NU 2216 EC
	140	33	187 000	245 000	31 000	4 000	4 800	2,05	NJ 2216 EC
	140	33	187 000	245 000	31 000	4 000	4 800	2,05	NUP 2216 EC
	170	38	260 000	280 000	36 000	3 200	3 800	3,35	NU 316 EC
	170	38	260 000	280 000	36 000	3 200	3 800	4,00	NJ 316 EC
	170	38	260 000	280 000	36 000	3 200	3 800	4,10	NUP 316 EC
	170	38	260 000	280 000	36 000	3 200	3 800	3,90	N 316 EC

Fig 7.5.2 Cylindrical roller bearings taken from SKF catalogue

Spherical roller bearings  
d 60-85 mm



Cylindrical bore

Tapered bore

Principal dimensions	Basic load ratings		Fatigue load limit $F_u$	Speed ratings		Mass	Designations Bearings with cylindrical bore	Designations Bearings with tapered bore	Calculation factors			
	dynamic	static		Lubrication	grease				oil	e	$Y_1$	
d	D	B	$C_0$	$C$	$N$	$n$						
mm			N	N		r/min	kg	-				
50	110	28	122 000	146 000	16 300	4 000	5 000	1,10	22212 CC	22212 CCK	0,24	2,8
	110	28	140 000	173 000	19 000	4 300	5 300	1,15	22212 E	22212 EK	0,24	2,8
	130	31	161 000	200 000	23 200	3 000	3 800	1,95	21312 CC	21312 CCK	0,24	2,8
	130	46	235 000	280 000	30 000	3 000	3 800	2,95	22312 CC	22312 CCK	0,35	1,9
	130	46	271 000	335 000	36 500	2 800	3 600	2,90	22312 E	22312 EK	0,35	1,9
65	120	31	148 000	180 000	21 200	3 600	4 800	1,45	22213 CC	22213 CCK	0,24	2,8
	120	31	176 000	216 000	24 000	3 800	4 800	1,50	22213 E	22213 EK	0,25	2,7
	140	33	184 000	240 000	27 000	2 800	3 600	2,45	21313 CC	21313 CCK	0,24	2,8
	140	48	253 000	300 000	32 000	2 800	3 400	3,55	22313 CC	22313 CCK	0,35	1,9
	140	48	299 000	360 000	38 000	2 600	3 400	3,55	22313 E	22313 EK	0,35	1,9
70	125	31	148 000	186 000	21 200	3 600	4 500	1,55	22214 CC	22214 CCK	0,23	2,9
	125	31	179 000	226 000	25 500	3 600	4 500	1,55	22214 E	22214 EK	0,23	2,9
	150	35	207 000	260 000	29 000	2 800	3 400	3,00	21314 CC	21314 CCK	0,24	2,8
	150	51	311 000	380 000	40 000	2 400	3 200	4,30	22314 CC/W33	22314 CCK/W33	0,35	1,9
	150	51	345 000	430 000	45 000	2 200	3 000	4,30	22314 E	22314 EK	0,33	2
75	130	31	158 000	208 000	23 600	3 400	4 300	1,65	22215 CC	22215 CCK	0,22	3
	130	31	184 000	240 000	26 500	3 400	4 300	1,70	22215 E	22215 EK	0,22	3
	150	37	235 000	300 000	32 500	2 400	3 200	3,55	21315 CC	21315 CCK	0,23	2,9
	150	55	345 000	430 000	44 000	2 200	3 000	5,25	22315 CC/W33	22315 CCK/W33	0,35	1,9
	150	55	385 000	476 000	48 000	2 200	3 000	5,25	22315 E	22315 EK	0,35	1,9
80	140	33	176 000	228 000	26 000	3 200	4 000	2,05	22216 CC	22216 CCK	0,22	3
	140	33	207 000	270 000	29 000	3 200	4 000	2,10	22216 E	22216 EK	0,22	3
	170	39	258 000	335 000	36 000	2 200	3 000	4,20	21316 CC	21316 CCK	0,23	2,9
	170	56	374 000	455 000	46 500	2 000	2 800	6,20	22316 CC/W33	22316 CCK/W33	0,35	1,9
	170	56	431 000	540 000	54 000	2 000	2 800	6,20	22316 E	22316 EK	0,35	1,9
85	150	36	210 000	270 000	31 000	3 000	3 800	2,55	22217 CC/W33	22217 CCK/W33	0,22	3
	150	36	244 000	325 000	34 500	2 800	3 500	2,65	22217 E	22217 EK	0,22	3
	180	41	293 000	375 000	40 000	2 000	2 800	5,00	21317 CC	21317 CCK	0,23	2,9
	180	60	420 000	520 000	52 000	1 900	2 500	7,25	22317 CC/W33	22317 CCK/W33	0,33	2
	180	60	477 000	620 000	61 000	1 900	2 500	7,25	22317 E	22317 EK	0,33	2

Fig 7.5.3 Spherical roller bearings taken from SKF catalogue



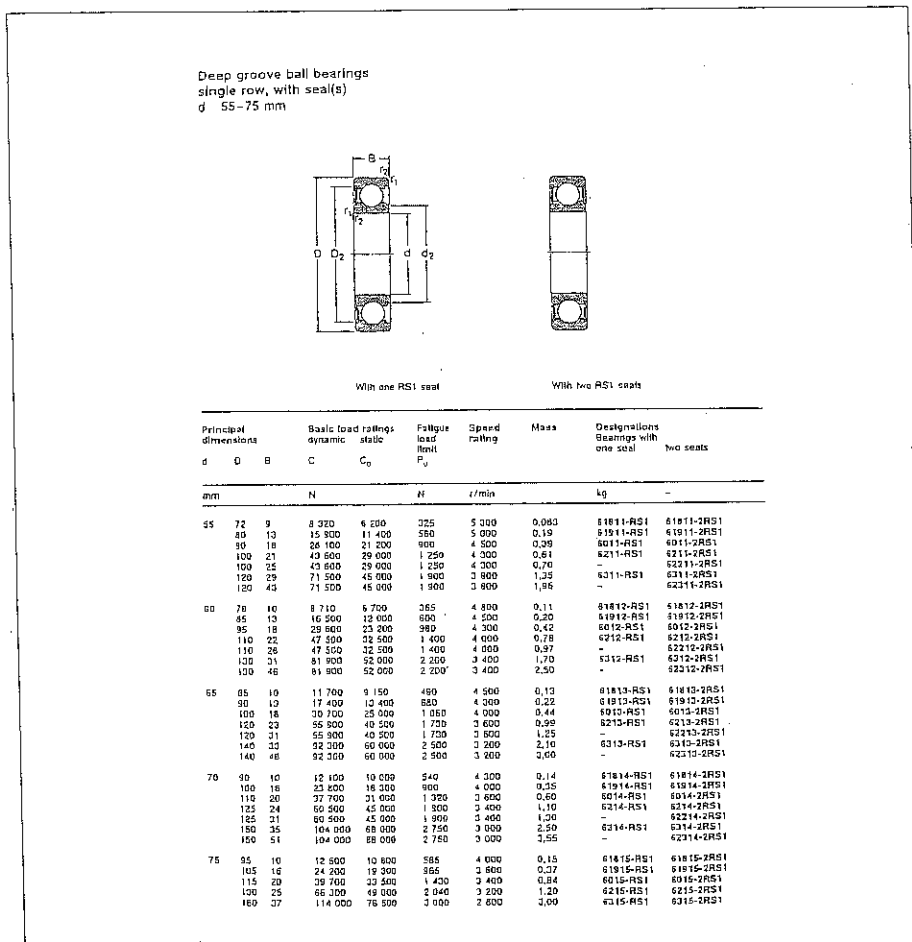


Fig 7.5.1 Deep groove ball bearings taken from SKF catalogue

Calculation factors X and Y for deep groove ball bearings

Table 7.5.2

The following is taken from SKF catalogue.

$F_a / C_0$	e	X	Y
0.025	0.22	0.56	2.0
0.04	0.24	0.56	1.8
0.07	0.27	0.56	1.6
0.13	0.31	0.56	1.4
0.25	0.37	0.56	1.2
0.50	0.44	0.56	1.0

The above values for X and Y apply when  $F_a / F_r > e$ . When  $F_a / F_r \leq e$  use  $X = 1$  and  $Y = 0$ .

Table 9.2.1

Discount factors for single sums

Period (n)	Discount rate (r)																											
	1%	2%	3%	4%	5%	6%	7%	8%	9%	10%	12%	14%	15%	16%	18%	20%	24%	28%	32%	36%								
1	0.9901	0.9804	0.9709	0.9615	0.9524	0.9434	0.9346	0.9259	0.9174	0.9091	0.8929	0.8772	0.8696	0.8621	0.8475	0.8333	0.8055	0.7813	0.7576	0.7353								
2	0.9803	0.9612	0.9426	0.9245	0.9070	0.8900	0.8734	0.8573	0.8417	0.8264	0.7972	0.7656	0.7561	0.7402	0.7162	0.6944	0.6504	0.6104	0.5739	0.5407								
3	0.9705	0.9423	0.9141	0.8859	0.8578	0.8296	0.8013	0.7731	0.7449	0.7167	0.6750	0.6375	0.6407	0.6066	0.5787	0.5245	0.4768	0.4348	0.3975	0.3643								
4	0.9610	0.9235	0.8855	0.8474	0.8092	0.7709	0.7326	0.6943	0.6560	0.6177	0.5685	0.5235	0.5215	0.4823	0.4430	0.3725	0.3284	0.2923	0.2563	0.2249								
5	0.9515	0.9037	0.8626	0.8214	0.7803	0.7392	0.6981	0.6570	0.6159	0.5748	0.5154	0.4722	0.4761	0.4371	0.4019	0.3411	0.2910	0.2485	0.2149	0.1860								
6	0.9420	0.8880	0.8375	0.7893	0.7422	0.7050	0.6683	0.6320	0.5963	0.5610	0.5065	0.4556	0.4333	0.4104	0.3704	0.3340	0.2751	0.2374	0.1980	0.1660								
7	0.9327	0.8706	0.8131	0.7599	0.7107	0.6651	0.6227	0.5833	0.5470	0.5132	0.4523	0.3996	0.3759	0.3526	0.3139	0.2791	0.2218	0.1776	0.1432	0.1162								
8	0.9235	0.8535	0.7884	0.7307	0.6768	0.6274	0.5820	0.5403	0.5019	0.4655	0.4056	0.3526	0.3285	0.3050	0.2660	0.2326	0.1769	0.1388	0.1085	0.0854								
9	0.9143	0.8366	0.7664	0.7026	0.6446	0.5919	0.5439	0.5002	0.4604	0.4241	0.3646	0.3075	0.2843	0.2630	0.2255	0.1938	0.1443	0.1084	0.0822	0.0628								
10	0.9053	0.8203	0.7441	0.6735	0.6139	0.5584	0.5083	0.4632	0.4224	0.3855	0.3220	0.2697	0.2472	0.2267	0.1911	0.1615	0.1164	0.0847	0.0623	0.0482								
11	0.8963	0.8043	0.7224	0.6466	0.5847	0.5266	0.4751	0.4289	0.3875	0.3505	0.2875	0.2366	0.2149	0.1954	0.1619	0.1366	0.0928	0.0662	0.0472	0.0340								
12	0.8874	0.7885	0.7014	0.6206	0.5568	0.4970	0.4440	0.3971	0.3555	0.3185	0.2567	0.2076	0.1869	0.1685	0.1372	0.1122	0.0707	0.0517	0.0357	0.0250								
13	0.8787	0.7730	0.6810	0.6006	0.5303	0.4688	0.4150	0.3677	0.3262	0.2897	0.2292	0.1821	0.1625	0.1452	0.1163	0.0925	0.0610	0.0418	0.0289	0.0200								
14	0.8700	0.7579	0.6611	0.5745	0.5081	0.4452	0.3907	0.3432	0.3017	0.2652	0.2057	0.1586	0.1397	0.1232	0.0965	0.0745	0.0482	0.0315	0.0215	0.0150								
15	0.8613	0.7430	0.6419	0.5503	0.4810	0.4173	0.3624	0.3152	0.2745	0.2384	0.1807	0.1340	0.1169	0.1019	0.0769	0.0563	0.0367	0.0247	0.0165	0.0115								
16	0.8528	0.7284	0.6232	0.5259	0.4581	0.3936	0.3387	0.2919	0.2510	0.2176	0.1631	0.1229	0.1069	0.0930	0.0708	0.0541	0.0320	0.0219	0.0118	0.0073								
17	0.8444	0.7142	0.6050	0.5134	0.4363	0.3714	0.3166	0.2700	0.2311	0.1978	0.1456	0.1078	0.0929	0.0802	0.0600	0.0451	0.0258	0.0159	0.0089	0.0054								
18	0.8360	0.7002	0.5874	0.4936	0.4155	0.3500	0.2952	0.2482	0.2109	0.1789	0.1300	0.0946	0.0803	0.0691	0.0508	0.0376	0.0208	0.0118	0.0069	0.0039								
19	0.8277	0.6864	0.5703	0.4745	0.3957	0.3305	0.2757	0.2317	0.1945	0.1635	0.1161	0.0829	0.0703	0.0595	0.0431	0.0315	0.0169	0.0092	0.0051	0.0029								
20	0.8195	0.6730	0.5537	0.4554	0.3769	0.3116	0.2584	0.2145	0.1784	0.1485	0.1037	0.0728	0.0611	0.0514	0.0355	0.0261	0.0135	0.0072	0.0039	0.0021								

To find the present value (PV) of a sum of money arising 'n' years in the future, given a discount or interest rate (r), multiply the future sum (FV) by the discount factor found in the table.

$$PV = FV \times \text{discount factor} = \frac{FV}{(1+r)^n}$$

Table 9.3.1

Discount factors for annuities

Period (n)	Discount rate (r)																											
	1%	2%	3%	4%	5%	6%	7%	8%	9%	10%	12%	14%	15%	16%	18%	20%	24%	28%	32%									
1	0.9901	0.9804	0.9709	0.9615	0.9524	0.9434	0.9346	0.9259	0.9174	0.9091	0.8929	0.8772	0.8696	0.8621	0.8475	0.8333	0.8055	0.7813	0.7576	0.7353								
2	1.9704	1.9416	1.9135	1.8861	1.8594	1.8334	1.8080	1.7833	1.7591	1.7355	1.6901	1.6467	1.6257	1.6052	1.5858	1.5276	1.4588	1.3916	1.3315	1.2745								
3	2.9410	2.8839	2.8288	2.7751	2.7232	2.6730	2.6243	2.5771	2.5315	2.4869	2.4018	2.3216	2.2832	2.2459	2.1743	2.1065	1.9813	1.8684	1.7633	1.6653								
4	3.9020	3.8077	3.7171	3.6299	3.5460	3.4651	3.3872	3.3121	3.2387	3.1669	3.0373	2.9137	2.8550	2.7982	2.6901	2.5847	2.4043	2.2410	2.0957	1.9577								
5	4.8534	4.7135	4.6797	4.6161	4.5295	4.4214	4.3002	4.1927	4.0887	3.9878	3.7908	3.6348	3.4331	3.3522	3.2743	3.1272	2.9066	2.7454	2.5320	2.3452								
6	5.7955	5.6014	5.4772	5.2421	5.0797	4.9173	4.7605	4.6229	4.4859	4.3353	4.1114	3.8887	3.7845	3.6847	3.4976	3.3255	3.0205	2.7594	2.5342	2.3320								
7	6.7282	6.4720	6.2903	6.0021	5.7864	5.5824	5.3993	5.2064	5.0320	4.8684	4.5238	4.2883	4.1904	4.0386	3.8115	3.6046	3.2423	2.9370	2.7075	2.5060								
8	7.6517	7.3225	7.0197	6.7327	6.4632	6.2099	5.9713	5.7488	5.5348	5.3348	4.9676	4.6389	4.4873	4.3436	4.0776	3.8372	3.4212	3.0758	2.7960	2.5851								
9	8.5660	8.1822	7.9031	7.6353	7.3788	7.1332	6.8981	6.6735	6.4595	6.2562	5.7990	5.3282	4.9664	4.7716	4.4865	4.0330	3.6410	3.2655	2.9542	2.6881								
10	9.4715	8.9926	8.5302	8.1109	7.7217	7.3601	7.0236	6.7101	6.4177	6.1446	5.6502	5.2181	5.0188	4.8332	4.4941	4.1825	3.6819	3.2889	2.9304	2.6129								
11	10.3676	9.7880	9.2528	8.7605	8.3064	7.8859	7.4987	7.1290	6.8052	6.4951	5.9377	5.4527	5.2337	5.0286	4.6550	4.3271	3.7757	3.3351	2.9776	2.6420								
12	11.2551	10.5753	9.9540	9.3851	8.8533	8.3638	7.9247	7.5361	7.1607	6.8137	6.1944	5.6909	5.4206	5.1971	4.7932	4.4392	3.8514	3.3684	3.0133	2.6590								
13	12.1337	11.3484	10.6350	9.9856	9.3936	8.8527	8.3577	7.9038	7.4869	7.1034	6.4235	5.8424	5.5631	5.3423	4.9095	4.5327	3.9124	3.4272	3.0404	2.6650								
14	13.0037	12.1092	11.2961	10.5931	9.9895	9.4350	8.9455	8.4422	7.9852	7.5667	6.8202	6.2021	5.9245	5.6755	5.0081	4.6106	3.9616	3.4567	3.0509	2.6529								
15	13.8658	12.8493	11.9379	11.1844	10.3797	9.7122	9.1079	8.5605	8.0507	7.6081	6.8109	6.1422	5.8474	5.5755	5.0916	4.6755	4.0013	3.4834	3.0764	2.6429								
16	14.7179	13.5777	12.5611	11.6523	10.8378	10.1059	9.4466	8.8514	8.3126	7.8237	6.9740	6.2651	5.9542	5.6885	5.1824	4.7296	4.0333	3.5028	3.0892	2.6252								
17	15.5623	14.2919	13.1661	12.1657	11.2741	10.4773	9.7632	9.1216	8.5435	8.0216	7.1196	6.3729	6.0472	5.7487	5.2223	4.7748	4.0591	3.5177	3.0971	2.5921								
18	16.3983	14.9920	13.7935	12.8593	11.9895	11.1696	10.4276	9.7591	9.1719	8.6358	7.2497	6.4674	6.1290	5.8176	5.2732	4.8132	4.0799	3.5294	3.1039	2.5589								
19	17.2260	15.6785	14.3238	13.3399	12.4853	11.5911	10.8356	10.2036	9.6501	9.1469	7.6359	6.5504	6.1962	5.8775	5.3162	4.8435	4.0667	3.5385	3.1050	2.5250								
20	18.0456	16.3514	14.8775	13.5903	12.6222	11.6698	10.9940	10.3461	9.7725	9.2516	7.6044	6.4231	6.2593	5.9268	5.3527	4.8898	4.1103	3.5458	3.1129	2.4929								

To find the present value of constant annual sums arising 'n' years in the future, given a discount or interest rate (r), multiply the repeated future sum (the annuity) by the discount factor found in the table.

$$PV = \text{annuity} \times \text{discount factor} = \text{annuity} \times \frac{(1+r)^n - 1}{r(1+r)^n}$$

BELT DRIVE CALCULATIONS 7.4

TABLE 3: SERVICE FACTORS

SPECIAL CASES	TYPES OF PRIME MOVER					
	Soft starts			Heavy starts		
	Electric Motors: AC - Star Delta start DC - Smart Wound Internal Combustion Engines with 4 or more cylinders All prime movers fitted with Centrifugal Clutches, Dry or Fluid Couplings or Electronic Soft Start devices			Electric Motors: AC - Direct-on-Line start DC - Series & Compound Wound Internal Combustion Engines with less than 4 cylinders Prime movers not fitted with soft start devices		
For speed increasing drives of: Speed ratio 1.00 - 1.24 multiply service factor by 1.00 Speed ratio 1.25 - 1.74 multiply service factor by 1.05 Speed ratio 1.75 - 2.49 multiply service factor by 1.11 Speed ratio 2.50 - 3.49 multiply service factor by 1.18 Speed ratio 3.50 and over multiply service factor by 1.25	Hours per day duty					
TYPES OF DRIVEN MACHINE	10 and under	Over 10 to 15	Over 15	10 and under	Over 10 to 15	Over 15
<b>Class 1</b> Light Duty Agitators (uniform density), Blowers, Exhausters and fans (up to 7.5 kW), Centrifugal compressors and pumps, Belt conveyors (uniformly loaded)	1.0	1.1	1.2	1.1	1.2	1.3
<b>Class 2</b> Medium Duty Agitators and mixers (variable density), Blowers, Exhausters and fans (over 7.5 kW), Rotary compressors and pumps (other than centrifugal), Belt conveyors (not uniformly loaded), Generators and excitors, Laundry machinery, Lineshafts, Machine tools, Printing machinery, Sawmills and woodworking machinery, Screens (dry)	1.1	1.2	1.3	1.2	1.3	1.4
<b>Class 3</b> Heavy Duty Brick machinery, Bucket elevators, Compressors and pumps (reciprocating), Conveyors (heavy duty), Hoists, Mills (hammer), Pulverizers, Funches, Presses, Shears, Quarry plant, Rubber machinery, Screens (vibrating), Textile machinery.	1.2	1.3	1.4	1.4	1.5	1.6
<b>Class 4</b> Extra Heavy Duty Cushers (gratory jaw roll), Mills (ball-rod-tube).	1.3	1.4	1.5	1.5	1.6	1.8

Power Ratings—SPC Wedge Belts

Revol/min of last shaft	RATED POWER (kW) PER BELT FOR SMALL PULLEY PITCH DIA (mm)																Belt Speed (m/s)	
	224	235	256	265	280	304	315	335	355	375	406	425	450	476	500	530		560
100	1.59	2.20	2.65	2.72	2.89	3.24	3.60	3.95	4.31	4.65	5.09	5.52	5.85	6.28	6.80	7.31	7.82	8.33
200	3.59	4.90	4.48	4.56	5.89	6.17	6.67	7.33	8.00	8.65	9.49	10.30	11.11	11.97	12.72	13.59	14.45	15.31
300	5.94	5.94	6.23	7.07	7.81	8.78	9.51	10.48	11.44	12.39	13.58	14.76	15.93	17.10	18.26	19.64	21.01	22.38
400	6.40	7.17	8.07	8.84	9.99	11.25	12.29	13.45	14.70	15.97	17.47	18.95	20.60	22.00	23.49	25.25	27.00	28.84
500	7.87	8.62	9.72	10.98	12.05	13.51	14.76	16.28	17.80	19.30	21.16	23.00	24.82	26.63	28.42	30.54	32.64	34.84
600	8.67	9.99	11.28	12.55	14.04	15.65	17.26	18.88	20.75	22.50	24.67	26.80	28.82	31.00	33.06	35.50	37.99	40.43
700	10.00	11.29	12.77	14.25	15.92	17.98	19.61	21.55	23.56	25.84	27.89	30.40	32.79	35.11	37.40	40.34	43.07	45.87
720	10.22	11.64	13.06	14.68	16.28	18.49	19.97	22.05	24.16	26.11	28.63	31.04	33.61	35.89	38.23	41.42	44.34	47.18
800	11.08	12.52	14.19	15.85	17.71	20.02	21.73	23.68	25.22	28.42	31.32	33.77	36.37	38.53	41.42	44.34	47.18	51.15
900	12.10	13.69	15.53	17.48	19.41	21.55	23.92	26.30	28.73	31.12	34.05	36.92	39.71	42.54	45.09	48.18	51.15	54.61
1000	12.65	14.36	16.26	18.25	20.25	22.65	25.02	27.41	30.18	32.65	35.71	38.68	41.56	44.38	47.12	50.27	53.29	56.81
1050	13.05	14.79	16.69	18.69	20.69	23.09	25.48	27.85	30.49	32.97	35.97	38.97	42.46	45.62	48.09	51.58	54.41	57.53
1100	13.56	15.31	17.21	19.21	21.21	23.61	25.98	28.35	31.09	33.57	36.57	39.57	42.46	45.62	48.09	51.58	54.41	57.53
1200	14.81	16.81	18.12	21.55	23.95	27.68	29.28	32.39	35.21	38.12	41.54	44.82	47.86	50.84	53.77	56.82	59.87	63.59
1300	16.58	17.72	20.17	22.74	25.91	29.06	31.97	34.89	37.12	40.05	43.66	46.90	50.05	52.92	55.79	58.68	61.59	64.59
1400	18.31	18.86	21.14	23.84	26.48	29.82	32.42	35.85	38.77	41.76	45.37	48.55	51.78	54.55	57.32	59.97	62.59	65.59
1440	18.59	18.86	21.59	24.25	26.84	29.43	32.86	35.23	38.37	42.28	45.21	49.71	52.22	54.22	56.22	58.22	60.22	62.22
1500	19.30	19.30	22.02	24.84	27.59	31.15	33.73	37.04	40.27	43.74	46.80	49.56	52.13	54.08	56.45	58.82	61.19	63.56
1600	17.58	20.03	22.83	25.75	28.59	32.24	34.98	38.26	41.45	44.41	47.98	51.03	54.08	56.45	58.82	61.19	63.56	65.93
1700	18.11	20.65	23.56	26.58	29.47	33.00	35.71	38.99	42.25	45.45	48.87	51.72	54.55	57.32	59.97	62.59	65.19	67.79
1800	18.57	21.20	24.18	27.25	30.23	34.01	36.71	39.99	43.25	46.15	49.43	52.13	54.82	57.51	60.20	62.89	65.58	68.27
1900	18.97	21.57	24.71	27.85	30.87	34.67	37.36	40.58	43.80	46.60	49.55	52.13	54.82	57.51	60.20	62.89	65.58	68.27
2000	19.29	22.06	25.15	28.34	31.27	35.18	37.84	40.96	44.09	46.72	49.35	52.13	54.82	57.51	60.20	62.89	65.58	68.27

Revol/min of faster shaft	ADDITIONAL POWER (kW) PER BELT FOR SPEED RATIO										
	1.00 to 1.01	1.02 to 1.05	1.06 to 1.11	1.12 to 1.18	1.19 to 1.26	1.27 to 1.38	1.39 to 1.57	1.58 to 1.84	1.85 to 2.24	2.25 to 2.75	2.76 to 3.39
100	0.00	0.02	0.06	0.11	0.14	0.17	0.20	0.23	0.25	0.26	0.26
200	0.00	0.04	0.12	0.21	0.28	0.35	0.41	0.46	0.50	0.53	0.53
300	0.00	0.07	0.18	0.32	0.43	0.52	0.61	0.68	0.73	0.79	0.79
400	0.00	0.09	0.24	0.42	0.57	0.70	0.83	0.92	1.00	1.08	1.08
500	0.00	0.11	0.30	0.53	0.72	0.87	1.02	1.15	1.25	1.32	1.32
600	0.00	0.12	0.33	0.57	0.76	0.96	1.04	1.22	1.37	1.50	1.59
700	0.00	0.15	0.42	0.74	1.03	1.22	1.43	1.63	1.89	2.10	2.19
720	0.00	0.16	0.43	0.76	1.03	1.26	1.46	1.66	1.84	1.80	1.80
800	0.00	0.17	0.48	0.84	1.15	1.39	1.61	1.83	2.00	2.11	2.11
900	0.00	0.20	0.54	0.95	1.29	1.56	1.85	2.06	2.26	2.35	2.35
1000	0.00	0.21	0.58	1.01	1.37	1.67	1.95	2.28	2.48	2.54	2.54
1050	0.00	0.23	0.60	1.05	1.43	1.74	2.04	2.25	2.50	2.59	2.59
1100	0.00	0.24	0.65	1.16	1.57	1.91	2.24	2.52	2.72	2.75	2.75
1200	0.00	0.26	0.72	1.25	1.72	2.09	2.44	2.75	3.00	3.00	3.00
1300	0.00	0.29	0.78	1.37	1.86	2.26	2.65	2.98	3.25	3.25	3.25
1400	0.00	0.31	0.84	1.47	2.00	2.43	2.85	3.21	3.60	3.60	3.60
1440	0.00	0.31	0.87	1.51	2.06	2.50	2.93	3.30	3.50	3.50	3.50
1500	0.00	0.33	0.90	1.58	2.15	2.61	3.05	3.44	3.75	3.75	3.75
1600	0.00	0.35	0.95	1.69	2.29	2.78	3.26	3.67	4.00	4.00	4.00
1700	0.00	0.37	1.02	1.79	2.43	2.96	3.46	3.90	4.25	4.25	4.25
1800	0.00	0.38	1.08	1.88	2.58	3.13	3.65	4.12	4.50	4.50	4.50
1900	0.00	0.42	1.14	2.00	2.72	3.20	3.87	4.25	4.76	4.76	4.76
2000	0.00	0.44	1.20	2.10	2.85	3.48	4.07	4.58	5.06	5.06	5.06

NOTE: Only pulleys of Fenner manufacture should be used where belt speed falls between 39 and 40 m/s.

Fig 7.4.1 Extracts from Fenner wedge belt catalogue continued from previous page

# Power Ratings—SPB Wedge Belts

Revolutions of faster shaft	RATED POWER KW PER BELT FOR SMALL PULLEY PITCH DIA (mm)														Belt Speed (m/s)
	140	150	160	170	180	190	200	212	224	235	250	260	270	280	
100	0.73	0.82	0.92	1.01	1.10	1.20	1.29	1.40	1.51	1.62	1.74	2.01	2.32	2.73	3.27
100	1.30	1.51	1.69	1.87	2.05	2.22	2.40	2.61	2.82	3.02	3.26	3.78	4.37	5.16	6.10
300	1.89	2.19	2.41	2.67	2.93	3.19	3.44	3.74	4.04	4.35	4.70	5.44	6.30	7.38	8.70
400	2.42	2.76	3.02	3.43	3.77	4.10	4.43	4.83	5.22	5.61	6.07	7.04	8.15	9.54	11.20
500	2.92	3.33	3.76	4.16	4.57	4.98	5.39	5.87	6.36	6.84	7.39	8.58	9.94	11.59	13.52
600	3.40	3.88	4.38	4.87	5.36	5.83	6.31	6.89	7.45	8.02	8.67	10.05	11.65	13.52	15.65
700	3.88	4.43	4.89	5.55	6.11	6.66	7.21	7.87	8.52	9.17	9.92	11.50	13.29	15.35	17.68
720	3.85	4.59	5.11	5.69	6.26	6.82	7.39	8.02	8.65	9.28	10.02	11.72	13.59	15.73	18.17
800	4.31	4.95	5.59	6.27	6.94	7.61	8.28	8.97	9.75	10.56	11.36	13.28	15.36	17.71	20.37
900	4.76	5.46	6.16	6.86	7.56	8.25	8.95	9.75	10.56	11.36	12.28	14.28	16.48	19.01	21.87
950	5.00	5.75	6.50	7.24	7.98	8.71	9.43	10.25	11.05	11.85	12.97	15.03	17.37	20.01	22.97
1000	5.17	5.95	6.72	7.49	8.25	9.01	9.76	10.55	11.33	12.10	13.42	15.55	17.95	20.65	23.65
1100	5.58	6.42	7.27	8.10	8.93	9.75	10.56	11.34	12.37	13.40	14.41	16.57	19.01	21.72	24.68
1200	5.97	6.82	7.75	8.55	9.39	10.22	11.02	11.80	12.68	13.59	14.78	17.06	19.69	22.57	25.68
1300	6.36	7.25	8.18	9.05	9.92	10.79	11.65	12.50	13.44	14.48	15.63	18.01	20.77	23.77	26.81
1400	6.73	7.77	8.81	9.83	10.84	11.84	12.82	13.99	15.14	16.27	17.57	20.08	22.78	25.81	28.97
1440	6.88	7.95	9.00	10.05	11.08	12.10	13.11	14.29	15.47	16.63	17.95	20.50	23.25	26.33	29.51
1500	7.08	8.20	9.29	10.37	11.44	12.49	13.63	14.76	15.97	17.15	18.51	21.10	23.90	27.01	30.22
1600	7.44	8.61	9.76	10.89	12.02	13.12	14.21	15.50	16.76	18.09	19.41	22.03	24.87	28.01	31.01
1700	7.78	9.01	10.21	11.40	12.58	13.73	14.87	16.21	17.52	18.91	20.27	23.27	26.17	29.17	32.23
1800	8.11	9.39	10.65	11.89	13.12	14.32	15.50	16.89	18.25	19.58	21.08	24.16	27.13	30.23	33.47
1800	8.43	9.76	11.08	12.37	13.64	14.88	16.11	17.54	18.94	20.31	21.85	24.93	27.95	31.01	34.71
2000	8.73	10.12	11.48	12.82	14.14	15.42	16.69	18.15	19.60	21.09	22.57	25.72	28.72	32.43	36.01
2100	9.02	10.46	11.88	13.26	14.52	15.84	17.14	18.75	20.22	21.74	23.24	26.41	29.37	33.01	37.21
2200	9.31	10.79	12.25	13.68	15.07	16.44	17.76	19.31	20.80	22.24	23.85	27.03	30.22	33.51	38.41
2200	9.57	11.11	12.61	14.08	15.51	16.89	18.25	19.83	21.35	22.80	24.42	27.57	30.69	34.01	39.61
2400	9.83	11.41	12.95	14.48	15.92	17.34	18.73	20.32	21.85	23.31	24.93	28.05	31.68	34.51	40.81
2500	10.08	11.70	13.20	14.82	16.21	17.76	19.16	20.77	22.31	23.78	25.41	28.78	32.17	35.01	42.01
2600	10.31	11.97	13.50	15.16	16.58	18.14	19.56	21.19	22.73	24.19	25.78	29.16	32.56	35.51	43.21
2700	10.53	12.23	13.81	15.47	16.91	18.50	19.93	21.55	23.11	24.58	26.12	29.54	32.95	36.01	44.41
2800	10.73	12.47	14.10	15.71	17.23	18.83	20.27	21.90	23.44	24.87	26.40	29.92	33.34	36.51	45.61
2800	10.88	12.65	14.35	15.88	17.57	19.07	20.51	22.14	23.97	25.08	26.67	29.92	33.34	36.51	45.61
2900	10.83	12.69	14.40	16.04	17.62	19.13	20.67	22.10	23.72	25.12	26.81	29.92	33.34	36.51	45.61
3000	11.10	12.90	14.63	16.20	17.88	19.40	20.94	22.36	23.98	25.33	27.06	29.92	33.34	36.51	45.61

Revolutions of faster shaft	ADDITIONAL POWER KW PER BELT FOR SPEED RATIO										
	1.00 to 1.01	1.02 to 1.05	1.05 to 1.11	1.12 to 1.18	1.19 to 1.26	1.27 to 1.38	1.39 to 1.57	1.58 to 1.94	1.95 to 2.38	2.39 to 2.98	3.00 to 3.57
100	0.00	0.01	0.02	0.04	0.04	0.06	0.07	0.07	0.08	0.09	0.09
200	0.00	0.01	0.04	0.07	0.09	0.11	0.13	0.15	0.16	0.17	0.17
300	0.00	0.02	0.05	0.10	0.14	0.17	0.20	0.22	0.23	0.24	0.24
400	0.00	0.03	0.07	0.13	0.19	0.22	0.26	0.28	0.29	0.30	0.30
500	0.00	0.04	0.09	0.17	0.23	0.28	0.33	0.37	0.40	0.43	0.43
600	0.00	0.04	0.12	0.20	0.26	0.34	0.40	0.46	0.50	0.51	0.51
700	0.00	0.05	0.13	0.24	0.30	0.39	0.46	0.54	0.60	0.62	0.62
720	0.00	0.05	0.14	0.25	0.33	0.41	0.48	0.54	0.62	0.65	0.65
800	0.00	0.06	0.15	0.28	0.37	0.46	0.53	0.60	0.69	0.72	0.72
900	0.00	0.07	0.16	0.31	0.41	0.51	0.60	0.69	0.78	0.81	0.81
950	0.00	0.07	0.18	0.32	0.44	0.54	0.62	0.70	0.79	0.81	0.81
1000	0.00	0.07	0.19	0.33	0.46	0.56	0.64	0.72	0.81	0.83	0.83
1100	0.00	0.08	0.22	0.37	0.51	0.62	0.72	0.81	0.89	0.91	0.91
1200	0.00	0.08	0.23	0.41	0.55	0.66	0.76	0.85	0.93	0.95	0.95
1300	0.00	0.09	0.25	0.44	0.60	0.71	0.81	0.90	0.98	1.00	1.00
1400	0.00	0.10	0.28	0.48	0.65	0.77	0.87	0.95	1.04	1.10	1.10
1440	0.00	0.10	0.28	0.48	0.65	0.77	0.87	0.95	1.04	1.10	1.10
1500	0.00	0.10	0.29	0.51	0.69	0.81	0.91	1.00	1.09	1.15	1.15
1600	0.00	0.11	0.31	0.54	0.75	0.89	1.00	1.10	1.19	1.26	1.26
1700	0.00	0.12	0.34	0.58	0.79	0.95	1.10	1.20	1.29	1.37	1.37
1800	0.00	0.13	0.35	0.61	0.84	1.01	1.16	1.26	1.34	1.45	1.45
1900	0.00	0.13	0.37	0.65	0.86	1.07	1.23	1.36	1.41	1.54	1.54
2000	0.00	0.14	0.38	0.68	0.93	1.13	1.32	1.48	1.52	1.68	1.68
2100	0.00	0.15	0.41	0.72	0.98	1.18	1.39	1.56	1.59	1.78	1.78
2200	0.00	0.16	0.43	0.76	1.02	1.24	1.45	1.63	1.63	1.85	1.85
2300	0.00	0.18	0.45	0.79	1.07	1.29	1.51	1.71	1.71	1.95	1.95
2400	0.00	0.17	0.47	0.82	1.11	1.33	1.58	1.78	1.78	2.04	2.04
2500	0.00	0.18	0.49	0.85	1.15	1.41	1.65	1.86	1.86	2.14	2.14
2600	0.00	0.19	0.51	0.89	1.21	1.46	1.72	1.92	1.92	2.19	2.19
2700	0.00	0.19	0.53	0.92	1.25	1.52	1.78	1.99	1.99	2.18	2.18
2800	0.00	0.20	0.54	0.95	1.29	1.57	1.84	2.07	2.07	2.18	2.18
2800	0.00	0.20	0.54	0.95	1.29	1.57	1.84	2.07	2.07	2.18	2.18
2900	0.00	0.21	0.57	0.99	1.34	1.63	1.91	2.15	2.15	2.24	2.24
3000	0.00	0.22	0.59	1.02	1.39	1.69	1.99	2.23	2.23	2.32	2.32

NOTE: Only pulleys of Fenner manufacture should be used where belt speed falls between 20 and 40 m/s.

Fig 7.4.1 Extracts from Fenner wedge belt catalogue continued from previous pages

BELT DRIVE CALCULATIONS 7.4

Table 1 Ideal class of pul/belt type and optimum diameter of the small pulley for new drives

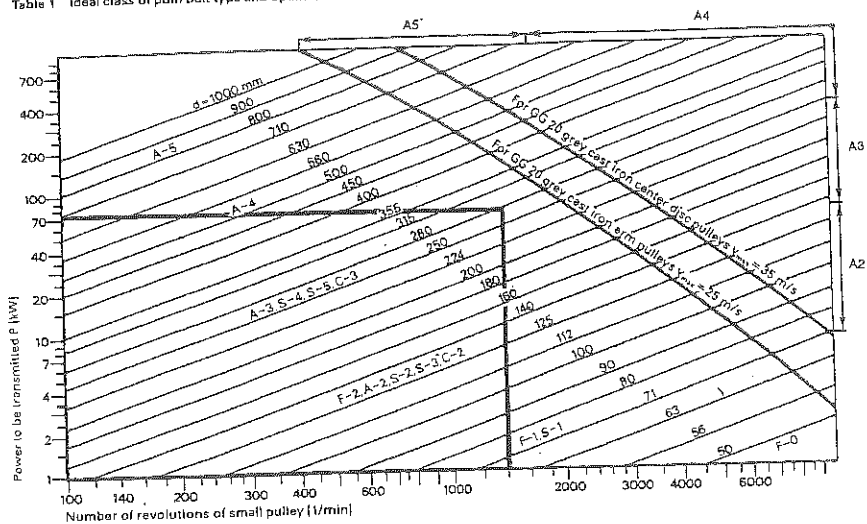


Table 2 Minimum center distance  $e_{min}$

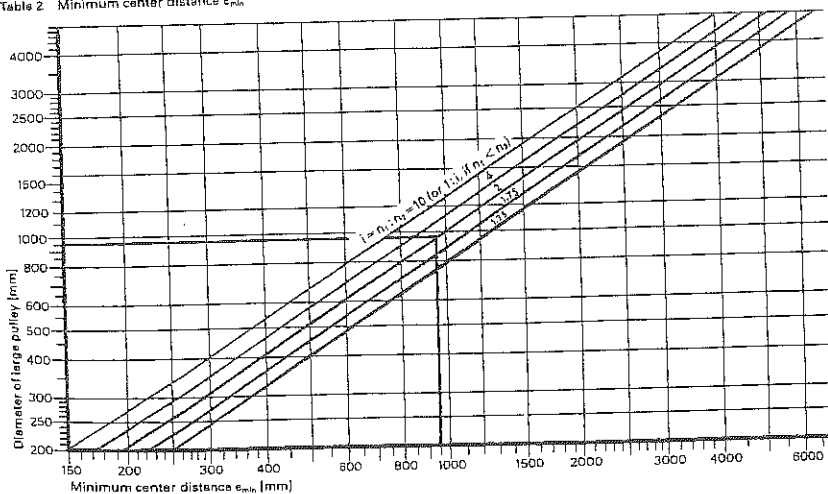


Fig 7.4.2 Extracts from Habasit catalogue continued on following pages

Fig 7.6.1 Torsion and bending

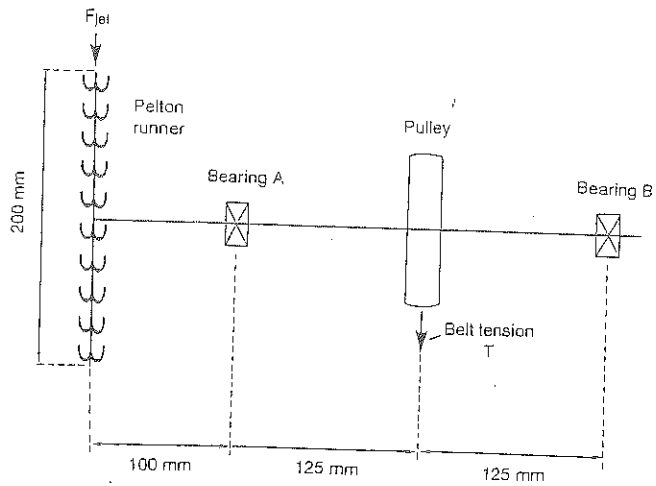


Fig 7.6.2 Pelton turbine and pulley drive. In this example the belt tension and turbine forces act in the same direction.

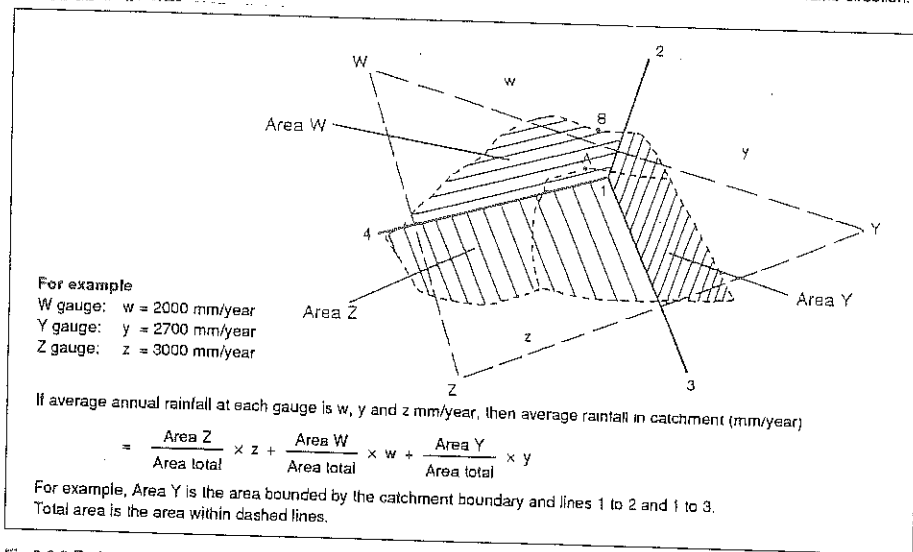


Fig 2.2.3 Estimating average rainfall